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# Quality Measures for Clusterwise Regression

Paula Brito, Sónia Dias, and Ndèye Niang

**Abstract** We focus on interval-valued variables, whose observations are intervals of real numbers. The Interval Distributional (ID) regression model [1] considers intervals represented by the corresponding quantile functions. The error between predicted and observed intervals, for each unit, is evaluated by the Mallows Distance. However, sometimes a single regression model is not appropriate, and it may be necessary to cluster the units and fit a regression model in each cluster. We apply a Clusterwise Regression model, for interval-valued variables, that finds the best partition of the data in clusters and simultaneously provides a linear regression model for each cluster. The algorithm [4], combines the dynamical clustering algorithm [2], and the ID regression model. The process is applied repeatedly varying the number of clusters  $K$ ; for each fixed  $K$ , the algorithm considers different initial partitions and selects the solution with lowest Total Error. To select the best solution across different  $K$ , quality measures are proposed, that evaluate the fit between the clusters and their representing regression models. In particular, we extend the well-known Silhouette coefficient to clusterwise regression. The proposed model and measures are applied to a problem of pollution prediction in West Africa.

**Keywords:** clusterwise regression, interval data, Silhouette coefficient

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